Section 1.2

1. Write $\neg(r \lor (q \land (\neg r \to \neg p)))$ in disjunctive normal form.

Solution Begin by giving the truth table for the statement:

p	q	r	$\neg r \rightarrow \neg p$	$q \land (\neg r \to \neg p)$	$r \vee (q \wedge (\neg r \to \neg p))$	$ \neg(r \lor (q \land (\neg r \to \neg p)))$
Т	Т	Т	Т	Т	Т	F
Т	Т	F	F	\mathbf{F}	\mathbf{F}	Т
Т	\mathbf{F}	Т	Т	\mathbf{F}	Т	F
Т	\mathbf{F}	\mathbf{F}	F	\mathbf{F}	\mathbf{F}	Т
\mathbf{F}	Т	Т	Т	Т	Т	F
\mathbf{F}	Т	F	Т	Т	Т	F
\mathbf{F}	\mathbf{F}	Т	Т	F	Т	F
\mathbf{F}	F	F	Т	\mathbf{F}	\mathbf{F}	Т

For each of the three true cases, form the conjunction that gives a T value only in that case: $p \land q \land \neg r$ $p \land \neg q \land \neg r$ $\neg p \land \neg q \land \neg r$.

Then form the disjunction of these three conjunctions to obtain the answer: $(p \land q \land \neg r) \lor (p \land \neg q \land \neg r) \lor (\neg p \land \neg q \land \neg r)$.